

## Term Structure of Interest Rates

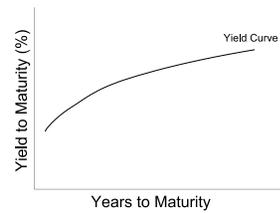
### Definition

Relationship between yield (market interest rate) and maturity for a specific type of bond ("Yield Curve")

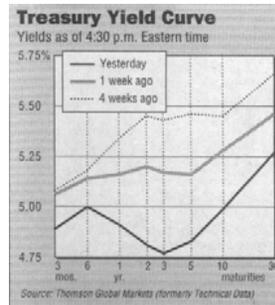
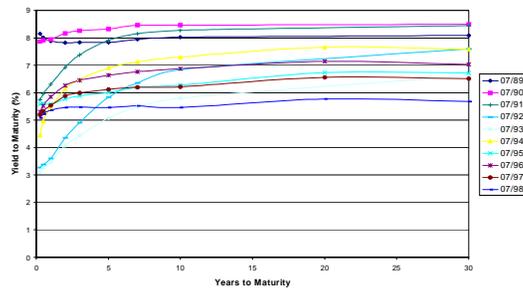
In constant motion [\[click\]](#), but normally slopes upward

### Issue

Does the shape of the Yield Curve mean anything?



U.S. Treasury Yield Curves



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## Term Structure Theories

### Market Segmentation

No: Long- and short-term rates not related; slope reflects only relative supply/demand for each type of bond. Yield Curve an optical illusion

Why: Maturity clienteles exist on both sides of market

### (Pure or Unbiased) Expectations

Yes: Long-term rates *averages* of short-term rates over same horizon (thus contain forecast of future interest rates)

Why: Borrowers/Lenders want best rate

### Liquidity Preference

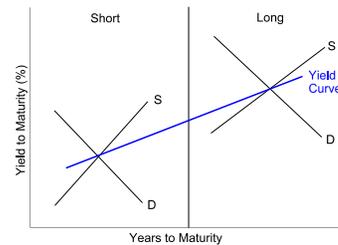
Yes: Long-term rates are averages of short-term rates plus *term premium* (MRP).

Why: Lenders prefer short-term bonds (less price risk, greater liquidity); accept lower rate  
Borrowers prefer long-term bonds (repayment less immanent); pay higher rate

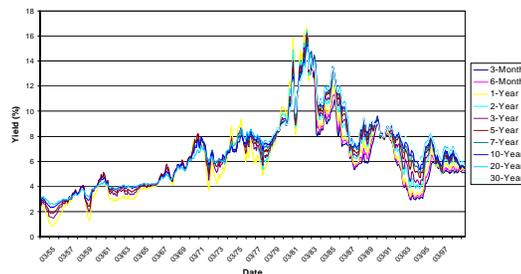
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## Market Segmentation

If the markets for long-term and short-term bonds are not related . . .



U.S Treasury Interest Rates



then why do they move together so closely?

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## Pure Expectations: Example

### Opportunities

| Rate on        | Observed Now | Expected in 1 Year |
|----------------|--------------|--------------------|
| 1-Year Loan/CD | 6.00%        | 10.00%             |
| 2-Year Loan/CD | 9.00%        |                    |

### Cash Flows

|       | 0       | 1     | 2     |
|-------|---------|-------|-------|
| Short | (1,000) | 1,060 | 1,166 |
| Long  | (1,000) | 1,090 | 1,188 |

### Strategy

Borrow where payoff lowest  
Lend where payoff highest

### Result

Rates converge until payoffs equalized (and 2-year rate is average of 1-year rates)

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## Pure Expectations: Equilibrium

### Opportunities

| Rate on        | Observed Now | Expected in 1 Year |
|----------------|--------------|--------------------|
| 1-Year Loan/CD | 8.00%        | 10.00%             |
| 2-Year Loan/CD | 9.00%        |                    |

### Cash Flows

|       | 0       | 1     | 2     |
|-------|---------|-------|-------|
| Short | (1,000) | 1,080 | 1,188 |
| Long  | (1,000) | 1,090 | 1,188 |

### Strategy

Maturity irrelevant

### Relationship

2-Year Rate is Average of the Two 1-Year Rates:  $k_2 \approx \frac{k_1 + \hat{k}_1}{2} = \frac{8\% + 10\%}{2} = 9\%$

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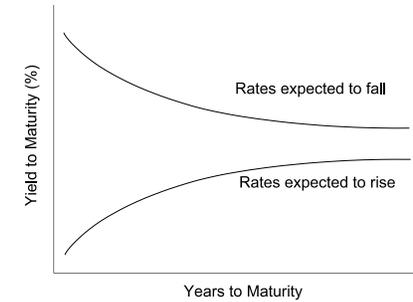
## Pure Expectations: Forecasting

If long-term rate is average of short-term rates:

- observe long-term rate and current short-term rate
- infer unobserved (expected) future short-term rate

### If Yield Curve: Rates are Expected to:

|             |                  |
|-------------|------------------|
| slopes up   | rise             |
| is flat     | remain unchanged |
| slopes down | fall             |



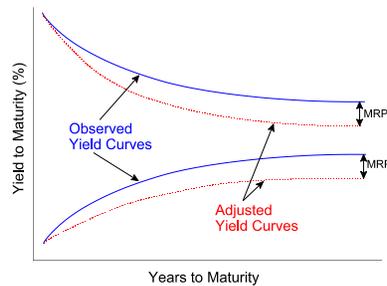
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## Liquidity Preference

If borrowers and lenders are *risk averse*, payoffs will *not* be equalized, because long-term rate includes risk premium, in addition to average of short-term rates:

$$k_2 \approx \frac{k_1 + \hat{k}_1}{2} + MRP$$

In order to forecast interest rate, first subtract unobserved MRP from observed yields



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