

## Cost of Capital

### Issue

What does it cost the firm to raise the next \$1 (or \$1 million)?

### Importance

Value Maximization minimize input costs  
 Capital Budgeting appropriate discount rate  
 Capital Structure optimum minimizes WACC

### Properties of Estimate

Marginal *new funds*  
 Average *all permanent financing target capital structure*  
 Market-based *investors' opportunity costs firm's floatation costs*  
 After-tax

## MCC Schedule

### Cost of Funds Depends on Amount Raised

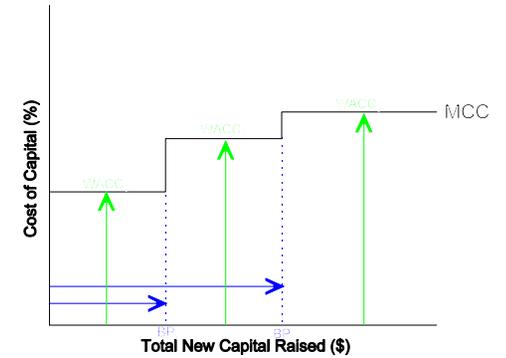
MCC vs. WACC  
 Breakpoint: Total can raise before cost rises

### Capital Components Involved

New Debt  
 New Preferred Stock  
 New Common Equity  
 Retained Earnings ("Internal")  
 Newly Issued Shares ("External")

### Limitations of Estimated MCC

Estimate valid only for given  
 capital structure  
 capital budget  
 dividend policy



## Estimating MCC

### WACC

$$WACC = k_a = w_d(1-T)k_d + w_{ps}k_{ps} + w_{cs}k_{cs}$$

$$w_i = \frac{\text{value of new capital of type } i}{\text{value of all new capital}}$$

### Breakpoint

$$BP_i = \frac{\$ \text{ amount available of capital of type } i}{w_i}$$

### Keeping Track of Estimates

Total New \$ Raised	Component Cost of:			WACC
	Debt	Preferred	Common	
Weight	$w_d$	$w_{ps}$	$w_{cs}$	

## Cost of New Debt

### Interest Deductible

Firm pays only after-tax cost:  $k_d^{AT} = \hat{k}_d(1-T)$

### Coupon Bond

Find like YTM (except for flotation cost  $f_d$ )

$$P_0^{net} = P_0(1-f_d) = \sum_{t=1}^{2n} \frac{\text{Int}/2}{\left(1+\frac{\hat{k}_d}{2}\right)^t} + \frac{M}{\left(1+\frac{\hat{k}_d}{2}\right)^{2n}}$$

### Zero-Coupon Bond

$$P_0^{net} = \frac{M}{(1+\hat{k}_d)^n}$$

### Perpetual Bond

$$k_d = \frac{\text{Int}}{P_0^{net}}$$

## Cost of New Preferred Shares

### Perpetual Preferred Stock

Find like expected return (except for flotation cost  $f_{ps}$ )

$$k_{ps} = \frac{D_p}{P_0^{net}} = \frac{\text{coupon rate} \times \text{par value}}{P_0(1-f_{ps})}$$

### Sinking Fund Preferred Stock

Find like cost of debt

$$P_0^{net} = \sum_{t=1}^n \frac{D_p}{(1+\hat{k}_{ps})^t} + \frac{\text{par value}}{(1+\hat{k}_{ps})^n}$$

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## Cost of Common Equity: Retained Earnings

### Opportunity Cost

No flotation cost, but not free capital

### Constant Growth

CAPM

$$k_{cs} = k_{RF} + (k_m - k_{RF})\beta_{cs}$$

DCF

$$k_{cs} = \frac{D_1}{P_0} + g = \frac{D_0(1+g)}{P_0} + g$$

BYPRP

$$k_{cs} = k_d + RP_{cs}$$

### Non-Constant Growth

$$P_0 = \sum_{t=1}^n \frac{D_t}{(1+\hat{k}_{cs})^t} + \frac{D_{n+1}}{\hat{k}_{cs}-g} \left[ \frac{1}{1+\hat{k}_{cs}} \right]^n$$

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## Cost of Common Equity: New Common Shares

### Note

Not issued until new retained earnings fully committed

### Constant Growth

Like expected return (except for flotation cost  $f_{cs}$ )

DCF

$$k_{cs} = \frac{D_1}{P_0^{net}} + g = \frac{D_0(1+g)}{P_0(1-f_{cs})} + g$$

### Non-Constant Growth

$$P_0^{net} = \sum_{t=1}^n \frac{D_t}{(1+\hat{k}_{cs})^t} + \frac{D_{n+1}}{\hat{k}_{cs}-g} \left[ \frac{1}{1+\hat{k}_{cs}} \right]^n$$

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## Extension: Project Risk

### Issue

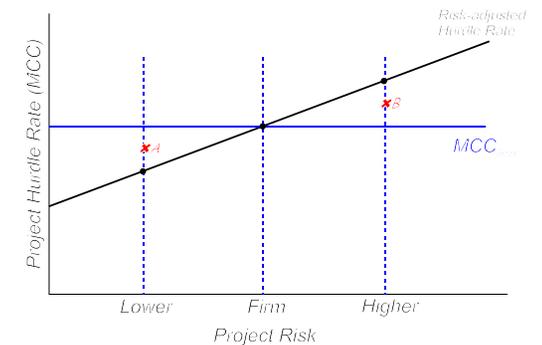
Which hurdle rate (MCC) to use in project evaluation?

$$NPV = \sum_{t=0}^n \frac{CF_t}{(1+MCC)^t}$$

### Importance

If rate too high, false rejection  
If rate too low, false acceptance

If ignore differential project risk, over time firm will become riskier, and its value will decline



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