

# Cost of Capital

## Issue

What does it cost the firm to raise the next \$1 (or \$1 million)?

## Importance

Value Maximization	minimize input costs
Capital Budgeting	appropriate discount rate
Capital Structure	optimum minimizes WACC

## Essential Properties of Estimate

Marginal	<i>new funds</i>
Average	<i>all permanent</i> financing target capital structure
Market-based	investors' opportunity costs firm's floatation costs
After-tax	

# MCC Schedule

## Cost of Funds Depends on Amount Raised

MCC vs. WACC

Breakpoint: Total can raise before cost rises

## Capital Components Involved

*New Debt*

*New Preferred Stock*

*New Common Equity*

Retained Earnings (“Internal”)

Newly Issued Shares (“External”)

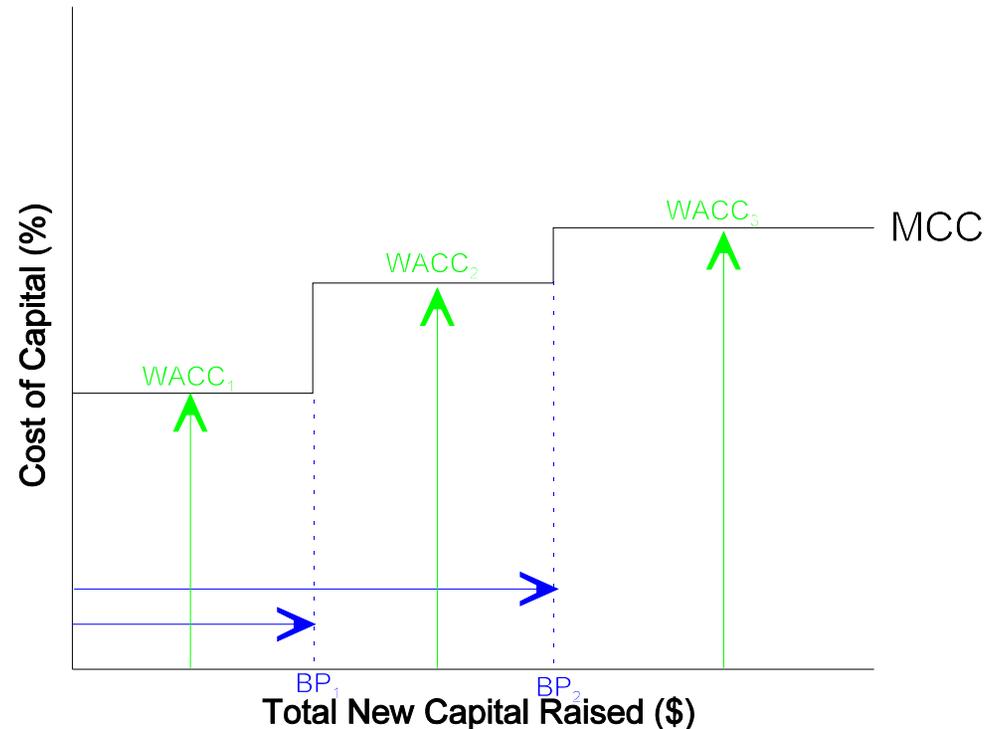
## Limitations of Estimated MCC

Estimate valid only for given

capital structure

capital budget

dividend policy



# Estimating MCC

## WACC

$$WACC = k_a = w_d(1-T)k_d + w_{ps}k_{ps} + w_{cs}k_{cs}$$

$$w_i = \frac{\text{value of new capital of type } i}{\text{value of all new capital}}$$

## Breakpoint

$$BP_i = \frac{\$ \text{ amount available of capital of type } i}{w_i}$$

## Keeping Track of Estimates

Total New \$ Raised	Component Cost of:			WACC
	Debt	Preferred	Common	

Weight                       $w_d$                        $w_{ps}$                        $w_{cs}$

# Cost of New Debt

## Interest Deductible

Firm pays only after-tax cost:  $k_d^{AT} = \hat{k}_d(1-T)$

## Coupon Bond

Find like YTM (except for flotation cost  $f_d$ )

$$P_0^{net} = P_0(1-f_d) = \sum_{t=1}^{2n} \frac{\text{Int}/2}{\left(1 + \frac{\hat{k}_d}{2}\right)^t} + \frac{M}{\left(1 + \frac{\hat{k}_d}{2}\right)^{2n}}$$

## Zero-Coupon Bond

$$P_0^{net} = \frac{M}{(1 + \hat{k}_d)^n}$$

## Perpetual Bond

$$k_d = \frac{\text{Int}}{P_0^{net}}$$

# Cost of New Preferred Shares

## Perpetual Preferred Stock

Find like expected return (except for floatation cost  $f_{ps}$ )

$$k_{ps} = \frac{D_p}{P_0^{net}} = \frac{\text{coupon rate} \times \text{par value}}{P_0(1-f_{ps})}$$

## Sinking Fund Preferred Stock

Find like cost of debt

$$P_0^{net} = \sum_{t=1}^n \frac{D_p}{(1+\hat{k}_{ps})^t} + \frac{\text{par value}}{(1+\hat{k}_{ps})^n}$$

# Cost of Common Equity: Retained Earnings

## Opportunity Cost

No flotation cost, but not free capital

## Constant Growth

CAPM

$$k_{cs} = k_{RF} + (k_m - k_{RF})\beta_{cs}$$

DCF

$$k_{cs} = \frac{D_1}{P_0} + g = \frac{D_0(1+g)}{P_0} + g$$

BYPRP

$$k_{cs} = k_d + RP_{cs}$$

## Non-Constant Growth

$$P_0 = \sum_{t=1}^n \frac{D_t}{(1+\hat{k}_{cs})^t} + \frac{D_{n+1}}{\hat{k}_{cs} - g} \left[ \frac{1}{1+\hat{k}_{cs}} \right]^n$$